| operator | $\|00\rangle$ | $\|01\rangle$ | $\|10\rangle$ | $\|11\rangle$ |
| :---: | :---: | :---: | :---: | :---: |
| $I_{1}$ or $I_{2}$ | $\|00\rangle$ | $\|01\rangle$ | $\|10\rangle$ | $\|11\rangle$ |
| $X_{1}$ | $\|10\rangle$ | $\|11\rangle$ | $\|00\rangle$ | $\|01\rangle$ |
| $X_{2}$ | $\|01\rangle$ | $\|00\rangle$ | $\|11\rangle$ | $\|10\rangle$ |
| $Z_{1}$ | $\|00\rangle$ | $\|01\rangle$ | $-\|10\rangle$ | $-\|11\rangle$ |
| $Z_{2}$ | $\|00\rangle$ | $-\|01\rangle$ | $\|10\rangle$ | $-\|11\rangle$ |
| $Y_{1}$ | $i\|10\rangle$ | $i\|11\rangle$ | $-i\|00\rangle$ | $-i\|01\rangle$ |
| $Y_{2}$ | $i\|01\rangle$ | $-i\|00\rangle$ | $i\|11\rangle$ | $-i\|10\rangle$ |
| $H_{1}$ | $\frac{\|00\rangle+\|10\rangle}{\sqrt{2}}$ | $\frac{\|01\rangle+\|11\rangle}{\sqrt{2}}$ | $\frac{\|00\rangle-\|10\rangle}{\sqrt{2}}$ | $\frac{\|01\rangle-\|11\rangle}{\sqrt{2}}$ |
| $H_{2}$ | $\frac{\|00\rangle+\|01\rangle}{\sqrt{2}}$ | $\frac{\|00\rangle-\|01\rangle}{\sqrt{2}}$ | $\frac{\|10\rangle+\|11\rangle}{\sqrt{2}}$ | $\frac{\|10\rangle-\|11\rangle}{\sqrt{2}}$ |
| $\Theta_{1}$ | $e^{i \theta}\|00\rangle$ | $e^{i \theta}\|01\rangle$ | $\|10\rangle$ | $\|11\rangle$ |
| $\Theta_{2}$ | $e^{i \theta}\|00\rangle$ | $\|01\rangle$ | $e^{i \theta}\|10\rangle$ | $\|11\rangle$ |
| $C n o t$ | $\|00\rangle$ | $\|01\rangle$ | $\|11\rangle$ | $\|10\rangle$ |
| common quantum operator rules |  |  |  |  |

