

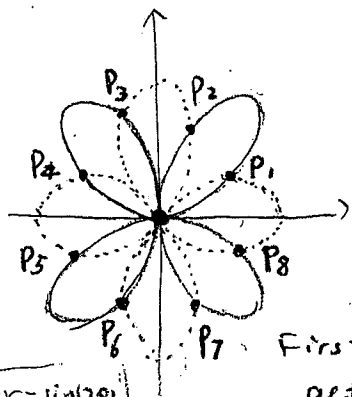
SHOW ALL WORK!!! Unsupported answers might not receive full credit. Use the back of this sheet for additional workspace.

Problem 1 [2 pts] Find all points of intersection for the polar curves $r = \sin(2\theta)$ and $r = \cos(2\theta)$.

$r = \sin(2\theta)$ and $r = \cos(2\theta)$ represent roses with four petals. The entire curves are generated as θ increases from 0 to 2π .

From the figure we should have 8 points of intersection.

From the way one graphs the two curves, some points of intersect are not achieved by the same θ -value. So we need to use some symmetry.



First solve $\sin(2\theta) = \cos(2\theta)$ or $\tan(2\theta) = 1$ to get $2\theta = \frac{\pi}{4}$ or $\theta = \frac{\pi}{8}$, so $r = \sin(2 \cdot \frac{\pi}{8}) = \frac{\sqrt{2}}{2}$.

Hence $P_1(\frac{\sqrt{2}}{2}, \frac{\pi}{8})$, $P_2(\frac{\sqrt{2}}{2}, \frac{3\pi}{8})$, $P_3(\frac{\sqrt{2}}{2}, \frac{5\pi}{8})$, $P_4(\frac{\sqrt{2}}{2}, \frac{7\pi}{8})$.

$P_5(\frac{\sqrt{2}}{2}, \frac{9\pi}{8})$, $P_6(\frac{\sqrt{2}}{2}, \frac{11\pi}{8})$, $P_7(\frac{\sqrt{2}}{2}, \frac{13\pi}{8})$, $P_8(\frac{\sqrt{2}}{2}, \frac{15\pi}{8})$, and

Problem 2 [2 pts] The equation of a certain polar curve is $r \sec \theta = 4$.

a) Find a description of the curve in terms of x and y .

$$r \sec \theta = 4 \Rightarrow r = 4 \cos \theta \Rightarrow r^2 = 4r \cos \theta$$

With $r^2 = x^2 + y^2$ and $x = r \cos \theta$, we get

$$x^2 + y^2 = 4x$$

$$\Leftrightarrow x^2 - 4x + y^2 = 0$$

$$\Leftrightarrow x^2 - 4x + 4 + y^2 = 4$$

$$\Leftrightarrow (x-2)^2 + y^2 = 2^2$$

the origin are all points of intersection.

b) Fill in the blanks:

The curve is a Circle of radius 2.

(centered at $(2, 0)$)